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The beta coefficient of an intermediate variable in a causal direction remains relatively constant as other system variables are introduced and controlled in stepped regression, whereas that in the acausal direction changes noticeably. Normalized random numbers (200x5) were generated and substituted in interdependent equations to produce five scores for each of 200 pseudo-people. Stepped-regression analysis was then applied on all possible three-variable paths. Beta differentials on a given intermediate variable were computed and compared for opposite directions. The resulting index persisted in yielding values between 0 and +1 in the one direction—the closer to 0, the stronger the direction—as other system variables were stepped in. But because some remaining three-variable paths imitated the known causal paths, further study was conducted to find support for the known causal paths, and to eliminate the imitations. Conclusions were that the beta index, found wanting initially, had greater utility as a confirming device, by the addition of the two modifications, in that all but the originally designed causal paths were eliminated as lacking causal-direction consistency. The index procedure may well be confined to the computer presently. (Author/GO)



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A BETA INDEX

TO CONFIRM CAUSAL DIRECTIONS

IN A CLOSED SYSTEM OF FIVE VARIABLES

By

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A BETA INDEX TO CONFIRM CAUSAL DIRECTIONS IN A CLOSED SYSTEM OF FIVE VARIABLES

ABSTRACT

The beta coefficient of an intermediate variable in a causal direction remains relatively constant as other system variables are introduced and controlled in stepped regression, whereas that in the acausal direction changes noticeably—the underlying intuitive principle of the study. The main strategy was to compare changes in beta coefficients of the intermediate variable from pairs of stepped equations in the causal direction to changes in the acausal direction of 3-variable paths.

200 x 5 normalized random numbers were generated and substituted in interdependent equations to produce 5 scores for each of 200 pseudo-people. Stepped-regression analysis was then applied on all possible 3-variable paths. Beta differentials on a given intermediate variable were computed and compared for opposite directions; the smaller of the two was treated as that of the causal direction and became the numerator of a beta index, and the larger became the denominator. The index persisted to obtain values between 0 and +1 in the one direction as other system variables were stepped in; the closer to 0, the stronger the causal direction.

But some remaining 3-variable paths imitated the known causal paths. Hence, further study was conducted to find support for the known causal paths and to eliminate the imitations. Comparisons of beta coefficients for end variables in regression equations and comparisons of correlations among the 3 path variables of known causal paths yielded mathematically-consistent like orders of magnitude as the beta differentials.

It was concluded that the beta index, found wanting initially, had greater utility as a confirming device by the addition of the 2 modifications in that all but the originally designed causal paths were eliminated as lacking causal-direction consistency. But obviously the index procedure might well be confined to the computer presently.



IN A CLOUED SYSTEM OF FIVE VARIABLES

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The researcher often has difficulty convincing himself and others about his findings on causal paths within a system of variables, regardless of rational conclusions, for he may not have included all relevant variables. Blalock, in pulling together materials on causal models, attempted to spell out the rules of causal inference, thus shortening the gap between theory and reality. His main strategy was to study beta coefficients in regression equations; such strategy served as the springboard for the present study.

In the exploratory construction of a Blalockian causal model, it was discovered that the beta coefficient of an intermediate variable in a causal direction remains relatively constant as other system variables are introduced and controlled in stepped regression, whereas that in the acausal direction changes noticeably—the beta constancy principle, upon which a beta index was developed as illustrated in Figure 1. For clearcut three-variable causal paths, the inequality between the magnitudes of the two beta differentials persisted, as remaining variables were stepped in, apparently a case of asymmetry emphasized by Blalock (p. 36); that is, the beta differential on the intermediate variable was less in the causal direction, or

$$d\beta_{c} < d\beta_{a} \tag{1}$$

But for other paths of connected variables, the inequality displayed inconsistencies such as reversals. The two members of the inequality were summarized in the form of a ration, called the beta index, such that the smaller of the two, treated as the beta differential for the causal direction, became the numerator. The value of this index, hence, was made to vary between +1 and 0; the closer to 0, the stronger the causal direction. From Inequality (1), therefore,

$$I_{\beta} = \frac{d\beta_{c}}{d\beta_{a}}$$
Insert Figure 1 about here

The problem then evolved as to whether the beta index could be demonstrated in a closed system of variables derived from dummy data and related by known causal paths by a system of equations.

METHOD

200 x 5 normalized random numbers (R_i) were generated and substituted into Equations 3 through 7 to obtain 5 scores (X_i) for each of 200 pseudopeople. These equations form the model portrayed in Figure 2, causal



directions indicated by arrows3.

 $X_1 = R_1 \tag{3}$

2

 $X_2 = R_2 \tag{4}$

 $x_3 = b_{31}x_1 + b_{32}x_2 + R_3 \tag{5}$

 $X_{l_{1}} = b_{l_{1}}X_{1} + b_{l_{1}}X_{2} + R_{l_{1}}$ (6)

 $X_5 = b_{52}X_2 + b_{511}X_{11} + R_5$ (7)

Insert Figure 2 about here

The b weights were set equal to 1 to find X_3 , X_{\parallel} , and X_5 , to simplify manipulation and analysis for the purpose of the present study. X_{\parallel} then served as input in stepped multiple-regression analysis, the output consisting of the required beta coefficients and other ancillary data.

In the initial stages of data processing, certain checks were conducted:
(1) the 5 x 5 R; correlation matrix revealed no r significantly different
from 0 at the .Ol level (see Table A); (2) the left and right members of
Equations 3 through 7 were found equal, to five significant figures, when
appropriate mean R; and mean X; were substituted (see Table B); and (3) the
b weights found in regression equations approximated the b weights in
Equations 3 through 7, with predicted X; and mean X; being found equal, to
five significant figures (see Table C).

Following rules outlined by Blalock (pp. 61-94), the X_1 correlations produced other checks to confirm the efficacy of the model, as outlined in Table 14. These final checks thus allowed further study of beta weights.

Insert Table 1 about here

Directions of the arrows in Figure 2 were disregarded initially in establishing possible causal directions in the three-variable paths. Nine paths were obvious: 132, 142, 145, 245, 254, 314, 324, 325, and 425, each clearly bi-directional. In the analysis, however, paths 145 and 245 were studied first, since they were the only two originally designed paths with causally connected (initial-cause, intermediate, and final-effect) variables.

The basic procedure included the following steps.

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- (1) A path of three variables was selected, and a causal direction was tentatively established, to include initial-cause, intermediate, and final-effect variables.
- (2) A pair of regression equations was found for the final-effect variable, predicted first by the intermediate variable alone and second with the initial-cause variable stepped in. The beta differential on the intermediate variable was then computed $(d\beta_c)$. In like manner, the beta

differential was computed for the acausal direction $(d\beta_a)$; that is, the initial-cause variable was predicted. The magnitudes of the two differentials were compared for order of value.

- (3) Step 2 was repeated, each time with one more of the remaining system variables stepped in and controlled. The end variable, initial-cause or final-effect, was always stepped in last to find the beta differential on the intermediate variable, such that the newly introduced variable was reflected in each of the pairs of equations. The beta differential was always taken on the original intermediate variable.
- (h) The decision was then made to retain or reject the causal direction established in Step 1, pending further study of imitations of known causal paths. If all comparisons of beta differentials from equation pairs in Steps 2 and 3 yielded the same order of value, the decision was made to retain.

The basic procedure was then switched to exploratory study of the imitations of known causal paths, such that (1) the magnitudes of end-variable beta coefficients were studied and (2) the magnitudes of the three correlation coefficients of the three-variable paths were studied. That is, a search was made for mathematical and logical consistencies.

The total variances in predicted variables X_3 , $X_{\downarrow i}$, and X_5 were then checked for contribution by component endogenous X_1 and exogenous R_1 .

Finally, in order to find explanation for apparent mathematical consistencies, the algebraic relations between beta and correlation coefficients were studied.

RESULTS

The study of beta differentials on intermediate variable X1 of path 115 is summarized in Table 2. First, comparison of A11 and A51, opposite directions, yielded nothing on which to base a decision as to causal direction. After the third (end) variable was stepped in for each direction, it was again noted that a comparison of betas, A11.5 and A51.1, yielded nothing for decision, and, in fact, the two sets of betas in predicting final variables were reversed in magnitude of values. However, the beta changes resulted in beta differentials which apparently supported the beta constancy principle. Obviously, the difference between A11 and A11.5, dA11 for the acausal direction was found to be greater than the difference between A51 and A51.1, dA51 for the causal direction. The change in slope (beta) of the intermediate variable was apparently relatively constant in predicting variable X5 (actually 21.5), but it was noticeably greater in predicting variable X1. Tentatively, the causal direction of path 11.5 was accepted as 1-1.5 rather than 5-1.1 (see Footnote 5). Since direction 1-1.5 was designed as causal, the decision appeared valid.

Insert Table 2 about here



When the fourth and fifth variables were stepped into regression and controlled, similar results were obtained. That is, the magnitude of days was found to be greater than days at each step, the intermediate variable being X1 and system variables X2 and X3 being introduced and controlled. It is emphasized that end variable X5 was stepped in last in predicting X1 for each equation pair; and X1, last in predicting X5.

The study of beta differentials on intermediate variable X_{l_1} of path $2l_15$ resulted in similar directional patterns as for path $1l_15$. At each step of analysis, the magnitude of $d\mathcal{A}_{2l_1}$ was greater than that of $d\mathcal{A}_{5l_1}$. Hence, the causal direction 2-4-5 was accepted (see Table 3).

What was expected for paths 145 and 245 as to directionality was actually found, that the beta coefficient on the intermediate variable in predicting the final-effect variable remained relatively constant while that in predicting the initial-cause variable (the opposite direction) changed noticeably.

The other seven paths were then analyzed, pertinent findings reported in Table 3, as derived from appropriate beta coefficients (see Table D). It was found that five directions, 2-3-1, 2-4-1, 2-5-4, 3-2-5, and 4-2-5, could also be causal based on beta-differential comparisons for all steps; that is, they imitated directions 1-4-5 and 2-4-5. Although directions 3-1-4 and 3-2-4 could be causal on the first two steps, they reversed on the last step of analysis (see Table 3), and hence, paths 314 and 324 were eliminated. From Figure 2, however, findings about the imitators could not be logical.

Insert Table 3 about here

Exploratory study of regression equations revealed some amplifying information about directions 2-5-4 and 4-2-5 which was similar to that about directions 1-4-5 and 2-4-5. The beta differentials for end variables, initial-cause and final-effect, compared the same as the beta differentials in like directions. For example, the magnitude of β_{51} was less than β_{15} for path 145 (see Table 2), at each step for all steps, just as d 54 was less than d 14, at each step for all steps. But obviously, directions 2-5-4 and 4-2-5 were not causal in design, and further differentiations would have to be made to eliminate them as causal. However, directions 2-3-1, 2-4-1, and 3-2-5 did not yield the same beta-coefficient patterns for end variables—and later they were found mathematically inconsistent—and were, therefore, not accepted as causal.

Because both zero-order and partial correlations could be misleading, the rationale of Blalock (pp. 65-77) was resorted to in analyzing the directions 1-4-5, 2-4-5, 2-5-4, and 4-2-5. The basic observation which Blalock (p. 73) attributes to others was then checked, that the magnitude of correlations between variables farthest apart in causal sequence should be smallest. At the same time, it was reasoned that the most recent relationship in the causal sequence should be greater in magnitude than any causally-prior relationship. (Together, these two points seemed to summarize the relationships among grandfather, father, and son over time.) In Table 4, zero-order correlations were first recorded, then followed by partials controlling for the effects of causally-prior variables having a direct effect on any of the two correlated variables. For the originally designed causal directions, 1-4-5 and 2-4-5,



it could be observed that the correlations between the initial-cause and final-effect variables, between the initial-cause and intermediate variables, and between the intermediate and final-effect variables were ascending in order of magnitude. For the remaining directions, 2-5-4 and 4-2-5, such order did not hold and hence they were rejected.

Insert Table 4 about here

The basic four-step procedure in finding beta differentials on which to base decisions as to causal directions seemed useful only for confirming but not for determining such directions, because many imitators were found. The refinements through study of end-variable beta coefficients and path correlations could conceivably strengthen the usefulness of the procedure, as supported mathematically in the discussion section.

As a confirming device, the beta index demonstrates that directions 1-4-5 and 2-4-5 are causal, as distinct from the acausal directions, in paths 145 and 245, respectively. Its utility was in question, however, despite its appeal to intuition, because of imitators found. Clearly then, if mathematical patterns could be determined beyond the basic four steps into exploratory study, and consistencies also found, persistent beta indices would have greater utility as confirming devices for causal directions in a closed system of variables, the model for which could be synthesized in different ways such as via Blalock.

DISCUSSION

Mathematics of Beta Differentials

Examination of causal direction 1-4-5 revealed the relationships in Inequalities 8, 9, and 10, the reduction of the beta-differential comparison to correlation comparison.

$$|\beta_{54} - \beta_{51-1}| < |\beta_{14} - \beta_{14-5}|$$
 (8)

$$\left|\mathbf{r}_{l_{1}5} - \frac{\mathbf{r}_{l_{1}5} - \mathbf{r}_{1}\mathbf{h}^{\mathbf{r}_{15}}}{1 - \mathbf{r}_{1}^{2}\mathbf{h}}\right| < \left|\mathbf{r}_{1}\mathbf{h} - \frac{\mathbf{r}_{1}\mathbf{h} - \mathbf{r}_{1}\mathbf{s}^{\mathbf{r}_{15}}}{1 - \mathbf{r}_{1}^{2}\mathbf{s}}\right|$$
 (9)

$$\left|\frac{\mathbf{r}_{11_{i}}}{1-\mathbf{r}_{11_{i}}^{2}}\right| < \left|\frac{\mathbf{r}_{1_{i}5}}{1-\mathbf{r}_{1_{i}5}^{2}}\right|$$
 (10)

Obviously, the most recent relationship in the causal sequence is greater in magnitude than the causally-prior relationship. Hence, the relationship

$$|r_{11}| < |r_{15}| \tag{10a}$$

must be true. The denominator of either member of Inequality 10, disregarding absolute-value symbols, serves to increase the value of the term curvilinearly, where r of +1 are the asymptotes; that is, the size of the correlation apparently increases (see Figure A).



Logically then, such a simple relationship as Inequality 10 could be very useful when causal relationships are initially studied; that is, by merely comparing correlations in a possible causal direction for three-variable paths. For the beta-differential comparisons to have any meaning, however, both Inequalities 8 and 10 must be true. But Inequality 10a must still be searched for.

when the fourth and fifth variables are reflected in beta-differential studies, the algebraic manipulations become extremely complicated to the point of becoming meaningless. However, geometric trace lines of hyperplanes may be pictured in the same manner as those in Figure 1. Reduction to simple correlations of higher-order beta coefficients is difficult, but this fact enhances the utility of beta differentials.

Mathematics of End-Variable Beta Coefficients

Examination of causal direction I-4-5 revealed further relationships in Inequalities 11 through 18.

$$|\beta_{51\cdot 4}| < |\beta_{15\cdot 4}| \tag{11}$$

which becomes

$$\left| \frac{\mathbf{r}_{15} - \mathbf{r}_{1i_1}\mathbf{r}_{15}}{\mathbf{1} - \mathbf{r}_{1i_1}^2} \right| < \left| \frac{\mathbf{r}_{15} - \mathbf{r}_{1i_1}\mathbf{r}_{15}}{\mathbf{1} - \mathbf{r}_{1i_5}^2} \right|$$

which simplifies to

Hence,

$$|\mathbf{r}_{11}| < |\mathbf{r}_{15}| \tag{12}$$

which is mathematically consistent with Inequality 10 and which now can be considered true. The end-variable beta coefficients must compare in order of magnitude the same as the beta differentials in like directions. At the same time, the most recent relationship in the causal sequence should be greater in magnitude than the causally-prior relationship.

In like manner, if

$$|\mathbf{\beta}_{51\cdot 2\mathbf{h}}| < |\mathbf{\beta}_{15\cdot 2\mathbf{h}}| \tag{13}$$

then

$$|\mathbf{r}_{14\cdot2}| < |\mathbf{r}_{15\cdot2}| \tag{14}$$

Tf

$$|\beta_{51\cdot 34}| < |\beta_{15\cdot 34}|$$
 (15)

then

$$|\mathsf{F1h.3}| < |\mathsf{Fh5.3}| \tag{16}$$



ľ

$$|\beta_{51\cdot23h}| < |\beta_{15\cdot23h}|$$
 (17)

then

$$|\mathbf{r}_{11\cdot 23}| < |\mathbf{r}_{15\cdot 23}|$$
 (18)

Obviously, the pattern in Inequalities 11 through 18 are all consistent with that in Inequalities 8 through 10. All values for these relationships were found for path 145.

All values for corresponding relationships were also found for path 245, the other causal path (see Tables D and E).

Extending the pattern of correlations of Inequalities 14, 16, and 18, it should follow that

$$|r_{11} \cdot 235| < |r_{15} \cdot 231|$$
 (19)

And then,

$$|\mathbf{r}_{14\cdot 25}| < |\mathbf{r}_{45\cdot 21}|$$
 (20)

$$|\mathbf{r}_{14..35}| < |\mathbf{r}_{45.31}|$$
 (21)

and

$$|\mathbf{r}_{1}| \cdot 5| < |\mathbf{r}_{1}| \cdot 5|$$
 (22)

Inequalities 19 through 22, in that they resemble and are consistent with Inequality 12, seemingly correspond to higher-order beta differentials much like Inequality 8 was simplified to Inequality 10. The mathematical relationships were not checked because of complicated intricacies, but nevertheless, the values for these relationships were found for path 145.

All values for corresponding relationships were also found for path 245, as indicated by Inequalities 19 through 22 for path 145 (see Table E).

All relationships for path 145 expressed in Inequalities 8 through 22 were found as well as correspondingly for path 245. And too, with the relationships found in Table 4, one becomes amused at the consistencies found for the causal directions as designed, whereas the other three-wariable paths display inconsistent patterns (see Table F). The patterns found that must be true are generalised in Table 5.

Insert Table 5 about here

Limitations of Mathematical Relationships

Although all mathematical relationships outlined hold for the designed causal directions 1-4-5 and 2-4-5, and although they apparently extend the beta constancy principle, they seem to detract from the original intent of demonstrating the beta index in confirming causal directions. But the side-step was exploratory. Heamwhile with the world not so mostly designed, cavest emptor.



Total Variances of Predicted Variances

Total variances for predicted variables X3, X1, and X5 are accounted for by both X4 and R4 (see Table 6). Obviously, 100% of the variance in each cannot be accounted for within the closed system of X4 alone. However, when appropriate R4 are stepped in, 100% of the variance of each predicted variable is achieved. Since the basic model of X4 in Figure 2 is less than ideal, the introduction of outside variables with X4 could change the beta-index concept, also a subject for later study. However, since most of the variance of each of the predicted variables at the final-effect end of a causal direction is accounted for within the system of X4, use of the beta index to confirm causal directions in exploratory models is considered adequate presently.

Insert Table 6 about here

Modifications

The four-step procedure for comparing beta differentials was repeated in two limited side studies: (1) with a horizontal distribution of R_i and (2) with randomized b coefficients in Equations 3 through 7. In the first, relationships in paths 1h5 and 2h5 were again found; whereas in the second, relationships in paths 1h5 and 2h5 were found inconsistent for many inequalities with beta indices approaching +1. It appeared that in the second study a symetry of beta differentials about the intermediate variable X_{li} was achieved, and the model, as modified, could not be causal at all. It appeared that further study of the causal model with a horizontal distribution of R_i could open other avenues for exploration of the utility of the beta index.

CONCLUSIONS

variable paths in a closed system of five variables was investigated and found wanting initially because of imitators. Relationships other than beta-differential comparisons, which made up the beta indices, in the same pairs of regression equations were derived and found to have mathematical consistency for designed causal directions, only two imitators remaining. Causal directions l-4-5 and 2-4-5, the two designed causal directions were still not eliminated when comparisons of the three correlations among the three path variables, with appropriate control for the effects of other system variables, yielded family-like order of values. A large number of combinations and permutations in the rive-variable system still exists unexplored, and obviously micro- and macro-scopic studies of same are indicated. It seems possible that with the present model of study, the beta index or at least its elements could find a way into causal theory. Presently, it appears it should be confined to the computer.



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FOOTNOTES

- 1. Now at Project COD (Title III ESEA, PL 89-10), 52 Ash Street, New Bedford, Mass. 02740.
- 2. Mathematics for this and other procedures were performed for the most part via programs for IBM 360 at the Boston College Computer Center. The present product was completed under the Title IV program (ESEA, PL 89=10) directed by Dr. John J. Walsh at the College.
- 3. The model was suggested by Dr. Ronald L. Nuttall, Associate Professor, Department of Psychology, Graduate School of Arts and Sciences, Boston College.
- 4. Blalock points out that a causal model is characterized by (1) a finite set of explicitly defined variables, (2) assumptions about how the variables are interrelated causally, and (3) assumptions to the effect that outside variables, while operating, do not disturb the causal patterning within the system. The present model meets these conditions; the design further makes the assumptions fact.
- for a given path of variables by numbers assigned. Later, numerical order is established for causal direction in the order given, with numbers hyphenated, to indicate initial-cause, intermediate, and final-effect variables, in their respective or reversed order. For the acausal direction, the reverse order should be obvious from context.
- 6. Ri are considered exogenous to the system of Xi in the actual causal model, although they are reflected in Equations 3 through 7; they are treated as if they are "random noise." It is also recognized that part correlations instead of partial correlations could have been explored where indicated in Figure 2.
- 7. Lettered tables and figures have been deposited with the American Documentation Institute. Order Document Number from ADI Auxiliary Publications Project, Photoduplication Service, Library of Congress, Washington, D. C. 205hO. Remit in advance for photocopies or for microfilm, and make checks payable to: Chief, Photoduplication Service, Library of Congress. Also see Educational Resources Information Center (ERIC) accession number ED_______.



TABLE 1 Correlation Checks for Model

1			Degrees (of Fit ^a	
Prediction Equation	Partial Control Value ^C		Actual Value	Expected	Valued
4-4	ъ	ъ	0109	ъ	ъ
r ₁₂ = 0	r15•24	0193	4269	ruirli2	5394
r ₃₄ = 0	r34+125	-1228	5781	r ₁₃ r ₁₁₁ + r ₂₃ r ₂₁₄	6477
r ₃₅ = 0	r _{35•12}	0134	5882	*23*25 + *23*24*45	6217

Note--Values are checked in two ways.

a Decimal points are omitted.

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- b Check is not necessary by design.

- c Value of partial approximates value of prediction equation. d Value of expected path approximates actual (zero-order) value. * At df of 200, $r_{01} \geq .181$ (see Arkin and Colton, pp. 24 & 155).

TABLE 2

Beta Studies for Path 145

				Compari	sons ^a			a s ah	
	1	Direction	n I-4-5 ^b			}	Direction	1 5-4:-10	Other d
Step	Other ^d Ii	ı	x _l	d/3	I _B	d/3	X _{l4}	15	Ii
1		-1822	8720 9847	1127	275	4093	6186 1.0279	- 4695	
24	2 2	0104	6755 6666	0089	262	037:0	85 1 4 8274	0355	2 2
2B	3	-2706	7989 9093	1104	262	4194	4080 9074	-6250	3
3	2, 3	0097	6728 6668	0060	بابانا	0135	6159 6024	0200	2, 3 2, 3

Note-Differentials are shown as positive values of differences.

a Decimal points are omitted for values below 1.

b Is is predicted.

c Ii is predicted.
d Other Ii are controlled in regression equations (see Table D).

TABLE 3

Beta Studies for Eight Paths

			2 3			
Other ^b	Direction ^c	d/3	I,s	d/3	Directionc	Causal Direction ^d
1, 3	2-4-5	1965 3181 2161 2425	202 338 151 382	9 721 9413 8368 6352	5-4-2	2 -1-2 2 -1-2 5 -1-2
4,5	1-3-2	2837 2722 2958 2474	765 725 371 479	2172 1975 1098 1185	2 -3-I	2-3-1 2-3-1 2-3-1 2-3-1
3 5 3, 5	1-4 -2	3172 3048 3480 5064	735 681 576 602	2328 2079 2 005 3050	2-4:-1	2-4-1 2-4-1 2-4-1 2-4-1
1 3 1, 3	2-5-li	1649 0387 1634 0050	427 549 405 563	3861 0704 4027 0088	4-5-2	2-5-4 2-5-4 2-5-4 2-5-4
2 5 2, 5	3-1-h	1841 0995 0338 0537	888 892 462 975	2073 1115 0727 0524	4-1-3	3-1-4 3-1-4 3-1-4 4-1-3
ī 5 1, 5	3-2-l:	2165 0863 0271 0507	977 908 299 158	2219 0951 0906 0080	4-2-3	3-2-4 3-2-4 3-2-4 4-2-3
1 4 1, 4	3-2-5	1491 0571 0019 0006	կ62 559 185 600	3228 1021 0103 0010	5-2-3	3-2-5 3-2-5 3-2-5 3-2-5
1 3 1, 3	4-2-5	3576 3484 2104 4055	473 615 372 675	7556 5664 5662 6020	5-2- ! :	4-2-5 4-2-5 4-2-5

Note-Follow Table 2 as model (see Table D for beta coefficients).

a Decimal points are omitted.

b Other Ii are controlled in regression equations.

c last number of the direction is that of the predicted variable; middle number, that of the intermediate variable from which d is derived.

d Tantative decision is based on I/3.



TABLE 4
Relationships of Variables in Causal Sequence

Causal Directionb (xyz)	Correlations ^a							
	Туре	CC	r _{xs}	Cc	rxy	Cc	r _{ys}	Causald
1-4-5	Zero-order Partial	Įŧ	4269 292 5	2	6186 7223	2	8720 8369	Yes
2-4-5	Zero-order Partial	1	7288 6652	L.	5293 6և33	12	8720 722 1	No
4-2-5	Zero-order Partial	2	8720 8369	1	5293 6652	L.	7288 6433	Жо

Note-See Tables A and E for other correlations.

a Decimal points are omitted.

b Directions are tentative from previous steps; the order of numbers in parentheses is to define correlations listed.

c The number listed is that of the variable controlled.

d Final decision is based on ascending order of correlations by columns from left to right.

from left to right.

At df of 200, $r_{01} \ge .181$ (see Arkin and Colton, pp. 2h & 155).



TABLE 5
Survey of Mathematical Consistencies

System	Control	Comp	parisons ^b	
Musber	Variables ²	Causal Direction	Acausal Direction	
1		Bcb - Bcb-a	Bab - Babec	(23)
		$\frac{\mathbf{r_{ab}}}{1-\mathbf{r_{ab}^2}}$	$\frac{\mathbf{r}_{bc}}{\mathbf{r}-\mathbf{r}_{bc}^2}$	(24)
		Bca-b	Bacob	(25)
		r _{ab}	r _{bc}	(26)
		r _{ab•c}	Pbc •a	(27)
2	d	Bebod - Beboda	Babed - Babede	(28)
		B ca bd	Bac ·bd	(29)
		rab •d	rcb •d	(30)
		Pab*ed	reb•ad	(31)
3	•	B cb .e - Bcb .ea	Babes - Babes	(32)
		Bcabe	Bac the	(33)
		rabee	r _{cp.e}	(孙)
		rat •ce	rcb-ae	(35)
4	d, •	Bebode - Bebodea	Bab-de - Bab-dec	(36)
		B ca-bde	Bac-bde	(37)
		^r ab de	rcb de	(38)
		Tab -cde	rcb-ade	(39)

Note—Generalisations were found for five-variable system and subsystems.

a This includes other than the ones included in three-variable paths.

b Causal direction, a-b-c, value is less than accusal direction, c-b-e, value for path abc with other system variables, d and e, introduced where appropriate; values are grouped vertically as comparisons of beta differentials on intermediate variables, beta coefficients of end variables, and other path correlations, respectively. Absolute-value symbols are omitted.

TABLE 6 Variance Accounted For by Ii and Ri

Predicted		Variance ^a							
Variance b	Y	AMEX	7-	V	total				
3·12) 3·67)°	3566	269L	•	-	6260				
3-128) 3-678)°	379 L	3060	3116	•	1,0000				
4·12) 4·67)°	3793	2766	•	•	6558				
4-129) 4-679)°	3835	30k2	3123	•	1,0000				
5-24	2705	5891	•	•	8596				
5-2410	2706	5890	11.04	•	1,0000				
5-679	1810	5535	1252	-	9597				
5-67930	2257	11 99	186 0	11/01	1.0000				

Note-Ri, where i is I through 5 in the original design, are set en variables 6 through 10, respectively, to facilitate their introduction into the system; variances are computed after Baggaley (p. 55), where total variance equals the sum of products of beta coefficient and respective carrelation for each term (predictor-predicted) in the regression system,

a Decimal points are cmitted for values below 1.

b The order of rembers in parentheses is to define components listed.

c I and I are the same as R1 and R2, respectively; hence, variables 6 and 7, respectively.

TABLE A Correlation Matrix of I_i and R_i

Variable	1	I					R _i			
Var	jeble	2	3	h _	5	1	2	3	<u>.</u>	5
I	1	0309	6001	6186	L269	1,9000	00.09	-062h	-0131	01.90
	2		5222	5293	7286	0209	1,0000	-1147	-0005	-0346
	3			5781	5005	6000	5222	5300	-1997	-00 L 7
	h.				8720	63.86	\$293	-1997	5300	-0112
	5					1,269	7288	-1763	3200	3542
1	1	1					020)	-4624	-0131	1250
	2							-1147	-0885	-0346
	3								-16.77	0057
	h.									0053

Note—Li are emberous variables; Ri, exercises; that is, internal and external, respectively, to the system.

a Decimal points are emitted for values below 1.

a At of of 200, rol > .181 (see Artin and Colton, sp. 24 & 155).

TABLE 5
Check of Hoose in Equations

Ba	notion	Left Hocher	Right Honber
			156.5522
	L		100.693h
	5	1478.4710	106.5521 + 108.6933 + 163.2257 - 1178.1681
	6	1479.304	166.5521 · 166.6933 · 163.5592 - 1179.1616
	7	2476.2700	150.6933 + 11.79.1714 + 150.1725 - 2176.2702



THEER C
Check of Home with Ingression Equations

Benetice	left their	Matt Medica
5	M.TS.ATM	-54-(166-5521) + .8800(168-1633) + 572-1638
		M6-95% - L38-85M - 572-6835 - 3L78-1685
6	1477.16A	.5005(Lot.5521) • .5005(Lot.4053) • 55L-7644
•		MOURE - 163-586 - 55-766 - 1675-1670
7	2.76.2700	JEN (LOR 4073) - 1,4055(1679,1066) - 500,6330
•		177.1436 - 147.2785 - 50.6379 - 127.2562

a liquitions are in the form of repression equations, such turn corresponding to the term of like variable in Equations 5, 6, and 7.

TABLE D Beta Coefficients of Predictor Xia

Predicted	cb x ₁	cb X2	Predictor X ₁ C ^b X ₃	c _p x ^f	c ^b X 5
1	-	- 0109 3 -4159 4 -4398 5 -6402 34 -6085 35 -7685 45 -4530 345 -6402	- 6001 2 8173 4 3643 5 5337 24 5618 25 6435 45 4432 245 5617	- 6186 2 8514 3 4080 5 1.0279 23 6159 25 8274 35 9074 235 6024	- 4269 2 8934 3 1129 4 -4695 23 6084 24 0355 34 -6250 234 0200
2	- 0109 3 -4727 4 -5127 5 -3671 34 -7472 35 -5544 45 -3385 345 -5582	-	- 5222 1 8059 4 3246 5 1430 14 5968 15 4388 45 1923 145 4397	- 5293 1 8465 3 3417 5 -4428 13 6465 15 -0948 35 -4951 135 0113	- 7288 1 8855 3 6147 4 1.1149 13 7073 14 9559 34 1.0474 134 6985
3	- 6001 2 5945 4 3928 5 4268 24 7060 25 6536 45 4995 245 7060	- 5222 1 5157 4 3003 5 1994 14 6108 15 6178 45 2900 145 6098		- 5781 1 3351 2 4192 5 2721 12 -1819 15 -2414 25 4005 125 -1836	- 5882 1 4060 2 4429 4 3510 12 -1410 14 5855 24 0276 124 0025
Ц	- 6186 2 6129 3 4245 5 3012 23 7124 25 2852 35 3350 235 3389	- 5293 1 5227 3 3128 5 -2263 13 6090 15 -0437 35 -2534 135 0070	- 5781 1 3234 2 4148 5 0997 12 -1674 15 -0791 25 1359 125 -0822		- 8720 1 7434 2 1.0369 3 8133 12 7821 13 7755 23 9767 123 7705
5	- 4269 2 4190 3 1154 4 -1822 23 4848 24 0104 34 -2706 234 0097	- 7288 1 7242 3 5797 4 3712 13 7813 14 3758 34 3693 134 3758	- 5882 1 5189 2 2855 14 1263 12 -1107 114 2219 214 0065 1214 0010	- 8720 1 9847 2 6755 3 7989 12 6666 13 9093 23 6728 123 6668	-

Note--This table is the basis for Tables 2 and 3.

a Decimal points are omitted for values below 1.

b The numbers are those of the variables controlled.

TABLE E Partial Correlation Matrix of Xi

Variable X _i	Сp	x ₂	C _p	x ₃	cp	XĮ,	c _p	15
1	- 3 4 5 34 35 45 345	0109 -4434 -4749 -4848 -6743 -6527 -3916 -5863	- 2 4 5 24 25 45 245	6001 6970 3783 3374 6298 6486 4705 6297	2 3 5 23 25 35 235	6186 7223 4162 5565 6624 4857 5513 4518	23h 23h 23h 23h	4269 6188 1142 -2925 5431 0193 -4113 0140
2			1 1 15 145 145	5222 6447 3122 1688 6037 5207 2362 5178	1 3 5 13 15 35 135	5293 6652 3269 -3166 6275 -0644 -3542 0089	1 3 4 13 14 34 134	7283 8008 6113 6433 7434 5994 6219 5119
3					2 5 1 12 15 25 125	5781 4170 1647 3292 -1745 -1382 2333 -1228	2 1 12 11, 21, 121,	5882 3556 2106 4590 -1249 3629 0134 0016
Ţ							1 2 3 12 13 23 123	8720 8556 8369 8061 7221 8398 8106 7168

a Decimal points are omitted. b The numbers are those of the variables controlled. * At df of 200, $r_{01} \ge .181$ (see Arkin and Colton, pp. 24 & 155).

TABLE F

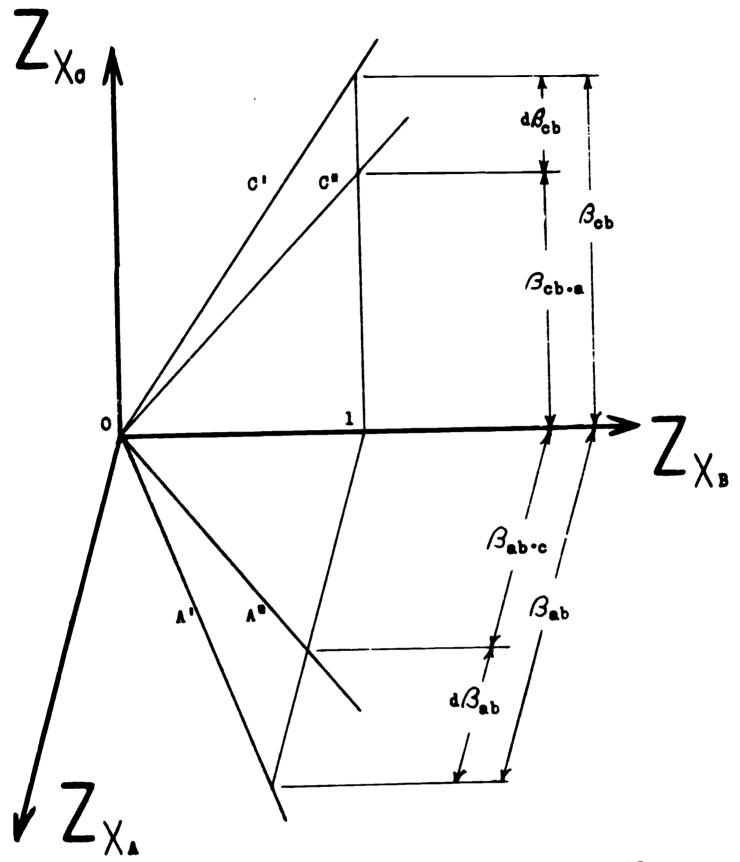
Mathematical Consistencies for Causal Directions

1	Selected Causal Directions ^b								
Comparisons	1-4-5	2-4-5	2-3-1	2-4-1	2-5-4	3-1-4	3-2-4	3-2-5	4-2-5
23	1	1	1	1	1	1	1	1	1
24	1	1	1	1	1	1	1	1	1
25	1	1	1	1	1	1	1	1	1
26	1	1	1	1	1	1	1	1	1
27	1	1	1	1	1	1	1	1	1
28	1	1	1	1	1	1	1	1	1
29	1	1	1	1	1	1	1	1	1
30	1	1	1	1_	1	1	1	1	1
31	1	1	1	1	1	1	1	1	1
32	1	1	1	1	1	1	1	1	1
33	1	1	0	ŋ	1	1	1	1	1
34	1	1	1	1	1	1	1	1	1
35	1	1	1	1	1	1	1	1	1
36	1	1	1	1	1	0	0	1	1
37	1	1	0	0	1	1	1	1	1
38	1	1	1	1	1	0	0	0	1
39	1	1	0	1	1	0	0	0	1

Note--For comparisons of actual values, see Tables 2, 3, A, D, and E. a Comparisons are those of Inequalities 23 through 39, as generalized in Table 5, in the same order.



b Causal directions were selected as a result of comparisons of first sets of beta differentials; that is, Inequality 23. Then I means YES that the comparison of actual values substituted makes the inequality true; 0, NO. Since another step is needed to eliminate two directions, 2-5-4 and 4-2-5, Table 4 is referred to.



Assume X_a causes X_b which causes X_c , in Path ABC. CAUSAL DIRECTION: A-B-C ACAUSAL DIRECTION: C-B-A

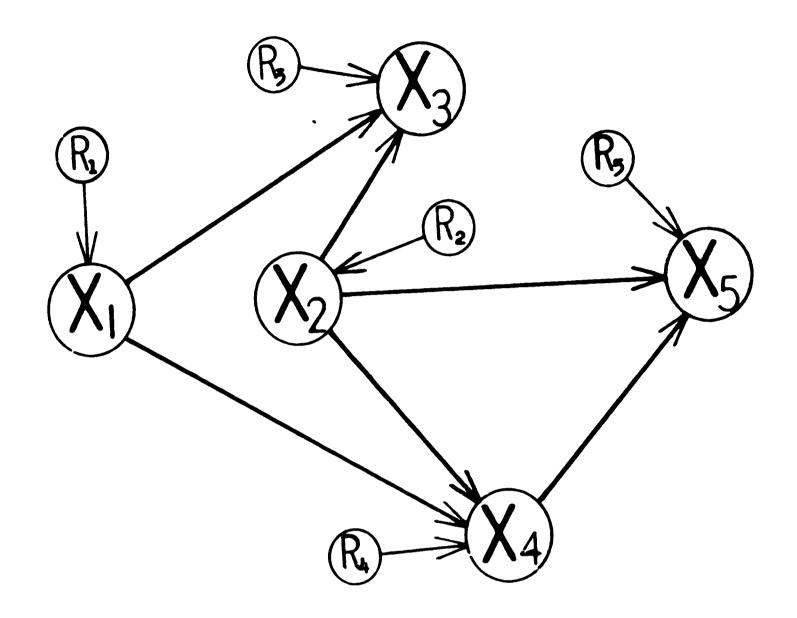
$$\frac{z_{X_{c}}}{z_{X_{c}}} = \beta_{cb} z_{X_{b}}$$

$$\frac{z_{X_{c}}}{z_{X_{c}}} = \beta_{cb} z_{X_{c}}$$

$$\frac{z_{X_{c}}}{z_{X_{c}}$$

FIGURE 1

THE BETA CONSTANCY PRINCIPLE AS BASIS FOR THE BETA INDEX



PEDURE 2

CAUSAL MODEL



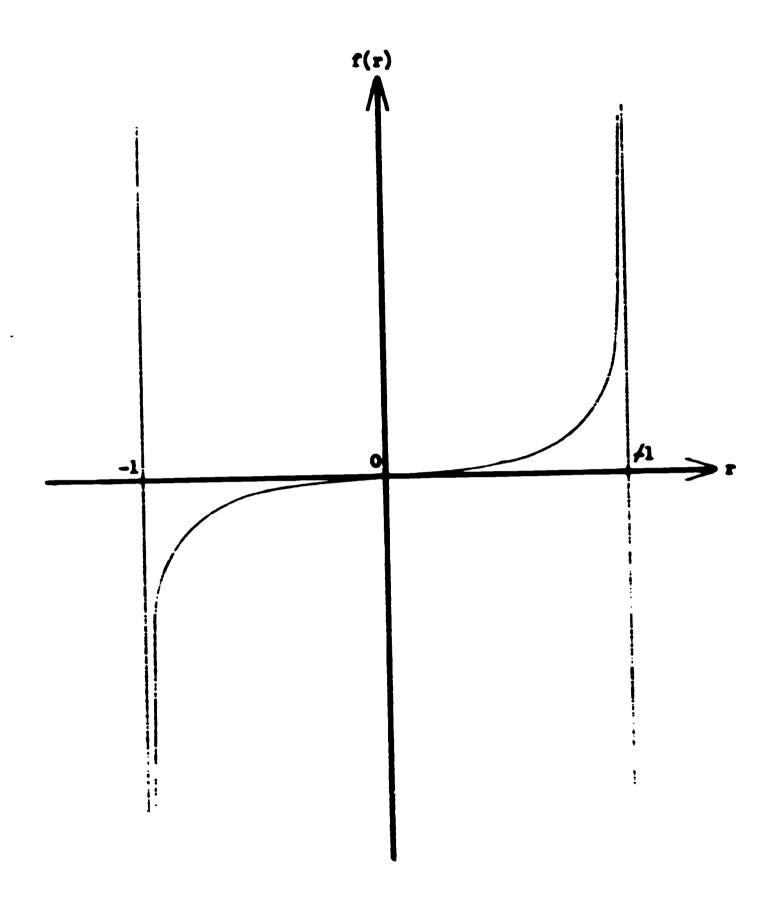


FIGURE A
FUNCTIONAL RELATIONSHIPS OF A STA-DIFFERENTIAL ELECTR



PART II

MEADING MANAGERIP?

Part II is for verbatin reading. It is a comionsation of Part I, which is the report of the stary itself, such that it may be read in 12-15 minutes. In order to charify main points while also ministrate brevity, four transparencies are reserved to, with overlaps as more surply for one with the courbood projector. Microphone and loudspeaker will be evailable for an expected attentance of 150 in the Try York Boom of the Statler Hilton Botel, 1:20-3:40 p.m., Friday, Pabromry 7, 1869. He assistance will be necessary, nor substitute reader. Or. Jerone 5. Deppe he of The Psychological Corporation is chairmen.



A BETA INDEX TO CONFIRM CAUSAL DIRECTIONS IN A CLOSED SYSTEM OF FIVE VARIABLES

READING MANUSCRIPT

GEORGE A. MIGRO

BOSTON COCLECE

GOOD AFTERWOOM, LADIES AND CENTLEMEN.

OTHERS ABOUT HIS PINDINGS ON CAUSAL PATHS WITHIN A SYSTEM OF VARIABLES, RECARDLESS OF RATIONAL CONCLUSIONS, FOR HE HAT NOT HAVE INCLODED ALL MELEVANT WARLANDES. MLALOCK, IN PULLING TOGETHER HATERIALS ON CAUSAL MODELS, ATTEMPTED TO SPELL OUT THE MULES OF CAUSAL IMPERENCE. HIS HALM STRATEGY WAS TO STOM BETA COMPTICIENTS IN REGRESSION EQUATIONS; HIS STRATEGY SZEVED AS THE SPRINGBOARD FOR THE PRESENT STORY.

MEMPLY, A CAMEAL MODEL INCLINES A PUBLIC SET OF EXPLICITLY MEPTIND VARIABLES, ASSUMED TO BE INTERMELATED CAMEALLY, ALONG LOGICALLY ASCENTALINED PATHS. IT IS ALSO ASSUMED THAT COTTSINE VARIABLES, WILLE OPERATING, BO NOT DISTORD THE CAMEAL PROTEINING WITHIN THE SYSTEM. THE VARIABLES IN THE SYSTEM NAVING CAMEAL MELATRONISHIPS AND NOT MEMBLY ASSOCIATED OR JOINED IN SUGLEMENT. BUT IF I PRODUCES Y, THEN ALSO A CAMEAR IN X PRODUCES A CAMEAR IN Y. IF THE YORK IS POSIND IMMORPHIES, THEN ADDITIONAL WARRANCES THAT YORK IS POSIND PROCESSED. AND POSINGE OF THE PARTIES.



IN THE EXPLONATORY CONSTRUCTION OF A MALACRIAN COLSIL.

HOGEL, IT WAS DISCOVERED THAT THE META COEFFICIENT OF AN INPERMEDIATE VARIABLE, IN A CAUSAL DIRECTION, MEMAINS MELATIVELY

COESTANT, AS OTHER VARIABLES AND INTRODUCED AND CONTROLLED IN

STEPPED RECRESSION: MEMAIS THAT IN THE ACMISAL DIRECTION CHARGES

MOTICEARLY—THE META CONSTRUCT PRINCIPLE, UPON MISCE A META INSET

MAS DEVELOPED, AS ILLUSTRATED IN FIGURE 1.

(TRASSPANENCY 1-1 3K.)

ASSUE THAT A-10-1C.

MERE ME MATE THE STANDARD-SCORE ALES FOR MAZIABLES & AND C.

LET C' METHESSENT THE LIME FOR PREDESTRING C FROM &. LET C' METHESSENT

THE LIME FOR PREPICTURE C FROM &. MET WITH A TREED MAZIABLE & STREPPED

DI AND CONTROLLES.

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THEMSPERSON 1-! OFFICER ...



LET US THERE HOP A PROPERDICTION FROM THE WILL FOR PRE-DECTION LINES TO A DESTRUCE OF 1 MILT PROPER THE MISSEN. ALONE THE AKES FOR § MEMORIEMENTS.

PROFESSIONAL 1-4 PROFESSIONAL

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CHARLES ! ST.

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CAUSAL DIRECTION; THAT IS, IN PREDICTING x_5 . WHEREAS, THE RIGHT SIDE OF THE TABLE INCLUDES THOSE FOR THE ACAUSAL DIRECTION; THAT IS, IN PREDICTING x_1 .

LOOK ACROSS THE TOP ROW OF STEP 1. NOTE THAT β_{54} IS GREATER THAN β_{14} —THEY TELL US NOTHING AS TO CAUSAL DIRECTION. IN THE SECOND ROW, THE THIRD, OR END, VARIABLE IS STEPPED IN FOR EACH DIRECTION, TO PREDICT x_5 AND x_1 . NOTE THE REVERSAL; THE NEW $\beta_{14\cdot 5}$ IS GREATER THAN $\beta_{54\cdot 1}$, BUT THEY STILL TELL US NOTHING AS TO CAUSAL DIRECTION.

BUT THERE ARE OBVIOUSLY CHANGES IN EACH DIRECTION. THESE CHANGES IN BETA COEFFICIENTS ARE THE BETA DIFFERENTIALS; $d/3_{54}$ IS OBVIOUSLY LESS THAN $d/3_{14}$. THE CHANGE IN THE DIRECTION OF PREDICTING x_5 , THE DESIGNED FINAL-EFFECT VARIABLE, IS LESS THAN IN THE OPPOSITE DIRECTION OF PREDICTING x_1 , THE DESIGNED INITIAL-CAUSE VARIABLE. THE TWO VALUES GIVE US A BETA INDEX OF .275, A VALUE CLOSE TO Q. TENTATIVELY THEN, BASED ON THE CONCEPT ALREADY DESCRIBED, DIRECTION $1\rightarrow 4\rightarrow 5$ IS CAUSAL.

(MOVE DOWN 1 STEP.)

IN LIKE MANNER, IN STEP 2A, A SYSTEM THAT INCLUDES A FOURTH VARIABLE, x_2 , is considered. In the top row, the first regression equation includes x_5 predicted from x_4 and x_2 first, and then with x_1 stepped in, on the second row. x_1 , on the right, is predicted from the same x_4 and x_2 , and then with x_5 stepped in. Note that x_2 is a system variable, but it is not listed, since it is not



STUDIED; ITS BETA COEFFICIENT MAY BE FOUND IN TABLE D. AGAIN THE BETA DIFFERENTIAL IS LESS IN PREDICTING X5 THAN X1, AGAIN FOR A LOW BETA INDEX.

(MOVE DOWN 1 STEP.)

STEP 2B REPEATS THE PROCEDURE FOR STEP 2A, BUT WITH SYSTEM VARIABLE X3 REPLACING X2.

(MOVE DOWN TO LAST STEP.)

LASTLY, STEP 3, THE SYSTEM FOR ALL 5 VARIABLES, INCLUDES

BOTH x_2 AND x_3 , BEFORE THE END VARIABLE IS STEPPED IN. IN EACH

SYSTEM OF INCREASING NUMBERS OF VARIABLES, THE BETA INDEX IS

CLOSE TO 0. THE BETA DIFFERENTIAL IN PREDICTING x_5 , THE DESIGNED

FINAL-EFFECT VARIABLE, IS LESS THAN THAT IN PREDICTING x_1 , THE

DESIGNED INITIAL-CAUSE VARIABLE. BASED ON THE BETA-INDEX CONCEPT,

DIRECTION $1\rightarrow 4\rightarrow 5$ PERSISTED AS CAUSAL.

(TRANSPARENCY 3 OFF.)

(TRANSPARENCY 2-1 ON AGAIN.)

PATH 245 RESULTED IN SIMILAR <u>BETA-DIFFERENTIAL</u> PATTERNS. IN OTHER WORDS, <u>WHAT WAS EXPECTED</u> FOR THE TWO CLEARCUT CAUSAL DIRECTIONS, $1\rightarrow4\rightarrow5$ AND $2\rightarrow4\rightarrow5$ IN THE DESIGN, <u>WAS FOUND</u>.



BUT <u>IMITATORS</u> OF THESE DESIGNED CAUSAL DIRECTIONS WERE ALSO FOUND, THUS WEAKENING THE <u>UTILITY</u> OF THE BETA INDEX.

EXPLORATORY STUDY OF REGRESSION EQUATIONS REVEALED SOME AMPLIFYING INFORMATION ABOUT DIRECTIONS 1-4-5 AND 2-4-5.

(TRANSPARENCY 2 OFF.)

THE BETA COEFFICIENTS FOR END VARIABLES COMPARED THE SAME AS THE BETA DIFFERENTIALS IN LIKE DIRECTIONS.

(TRANSPARENCY 3 ON AGAIN.)

NOTE THAT THE BETA COEFFICIENT OF x_1 , IN PREDICTING x_5 , IS LESS THAN THAT OF x_5 IN PREDICTING x_1 , AT EACH STEP IN THE TABLE. BUT DIRECTIONS 2-5-4 AND 4-2-5 STILL HELD UP AS IMITATORS OF 1-4-5 AND 2-4-5. UTILITY OF THE BETA INDEX REMAINED IN QUESTION.

(TRANSPARENCY 3 OFF.)

BLALOCK OBSERVED THAT THE CORRELATION BETWEEN VARIABLES

FARTHEST APART IN CAUSAL SEQUENCE SHOULD BE SMALLEST. IT WAS ALSO

REASONED THAT THE MOST RECENT RELATIONSHIP IN THE CAUSAL SEQUENCE

SHOULD BE GREATER IN MAGNITUDE THAN ANY CAUSALLY PRIOR RELATIONSHIP.

TOGETHER, THESE TWO POINTS SEEMED TO BE SIMILAR TO THE FAMILY-LIKE



RELATIONSHIP AMONG GRANDFATHER, FATHER, AND SON OVER TIME. SUCH RELATIONSHIPS, WITH APPROPRIATE CONTROLS FOR THE EFFECTS OF OTHER SYSTEM VARIABLES, WERE FOUND ONLY FOR DIRECTIONS 1—4—5 AND 2—4—5. THIS FINDING SEEMS TO EMANATE MIXED FEELINGS ABOUT THE BETA INDEX. BY A SCREENING PROCEDURE, THE TWO DESIGNED DIRECTIONS IN CAUSAL SEQUENCE OF 3-VARIABLE PATHS HELD UP, YET ONE WONDERS IF CORRELATIONS ALONE COULD BE STUDIED TO CONFIRM CAUSAL DIRECTIONS. BUT THE ONE FORMIDABLE OBSTACLE IN SUCH STUDY WOULD BE TO PLAY CHESS ON A CORRELATION MATRIX INCLUDING ALL PARTIALS.

THE MATHEMATICS WERE THEN STUDIED TO FIND OUT WHY THE BETA INDEX AND END-VARIABLE BETA COEFFICIENTS WERE PERSISTENTLY PATTERNED FOR CAUSAL DIRECTIONS.

DISCUSSION

THE MATH IS TREATED IN DETAIL IN THE DISCUSSION SECTION OF YOUR PAPER. NOTE INEQUALITY 8 FOR BETA DIFFERENTIALS AND INEQUALITIES 11, 13, 15, AND 17 FOR END-VARIABLE BETA COEFFICIENTS. BUT MOST REVEALING, AND SUPPORTIVE TO THE IDEA OF CORRELATIONAL STUDY, ARE INEQUALITIES 10, 12, 14, 16, AND 18, DERIVED FROM CORRESPONDING BETA COMPARISIONS, AND INEQUALITIES 19—22, ARRIVED AT BY LOGIC. THESE COMPARISONS ARE SUMMARIZED IN TABLE 5 FOR SYSTEMS OF 3, 4, AND 5 VARIABLES; THEY ARE ALSO GENERALIZED HERE.

(TRANSPARENCY 4 ON.)



ASSUME CAUSAL DIRECTION A-B-C IN A SYSTEM. THESE INEQUALITIES WOULD SEEM TO HOLD TRUE, WHERE K MAY BE ZERO OR MORE OTHER RELEVANT VARIABLES, CONTROLLED IN THE SYSTEM. ALSO NOTE THE FAMI-LY-LIKE COMPARISONS OF CORRELATIONS FOR DIRECTION A-B-C.

(TRANSPARENCY 4 OFF.)

CONCLUSIONS

THE PROBLEM OF USING A <u>BETA INDEX</u> TO CONFIRM CAUSAL DIRECTION WAS INVESTIGATED AND FOUND <u>WANTING INITIALLY</u> BECAUSE OF IMITATORS.

OTHER RELATIONSHIPS WERE FOUND THAT DISPLAYED MATHEMATICAL

CONSISTENCY FOR DESIGNED CAUSAL DIRECTIONS. THESE POINTED IN THE

DIRECTION OF CORRELATIONAL RATHER THAN BETA STUDY.

ALTHOUGH THE BETA-INDEX CONCEPT IS STRONGLY SUPPORTED, ITS USAGE MIGHT WELL BE CONFINED TO COMPUTERS PRESENTLY.

THE ELEMENTS OF THE INDEX, HOWEVER, THE INEQUALITIES, SHOULD BE CONSIDERED IN THE STUDY OF OTHER CAUSAL MODELS.

THE REAL ADVANTAGE OF THE BETA INDEX OVER CORRELATIONAL STUDY
SEEMS TO BE IN TAKING OUT THE CHESSBOARD FRUSTRATION OF INSPECTING
A CORRELATION MATRIX THAT INCLUDES ALL PARTIALS. IN ANY EVENT, THE
STUDY SEEMS TO HAVE BEEN WORTHWHILE AND PERSONALLY INTERESTING.

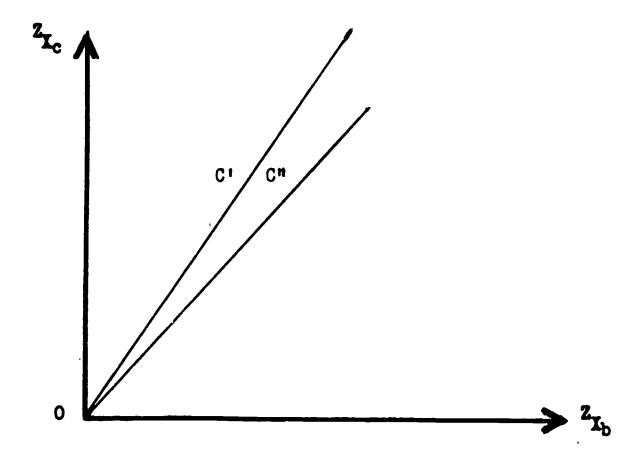
IN LEADING THE CAUTIOUS, PATIENT LISTENER AROUND ROBIN HOOD'S BARN, THE AUTHOR HOPES THAT SOME BENEFIT HAS BEEN DERIVED FROM THE

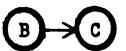


PRESENTATION. AS A PROFESSOR ONCE SAID AT THE END OF HIS LONG LECTURE, "THE LONGER THE SPOKE, THE GREATER THE TIRE."

THANK YOU.

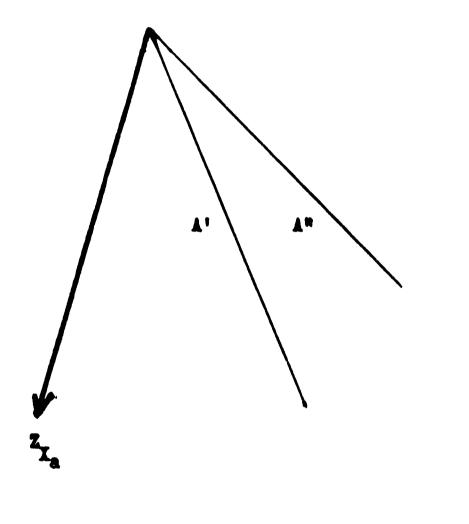






TRANSPARENCY 1-1



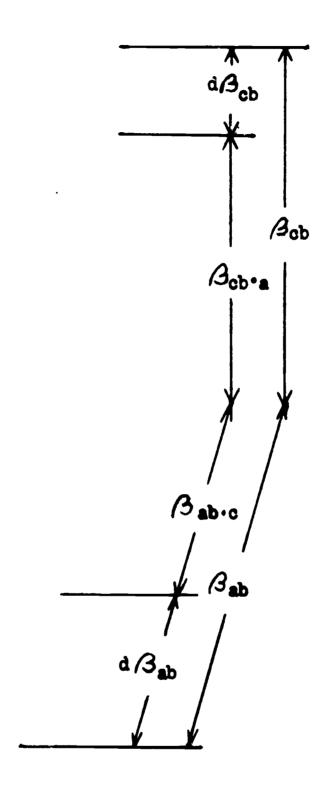




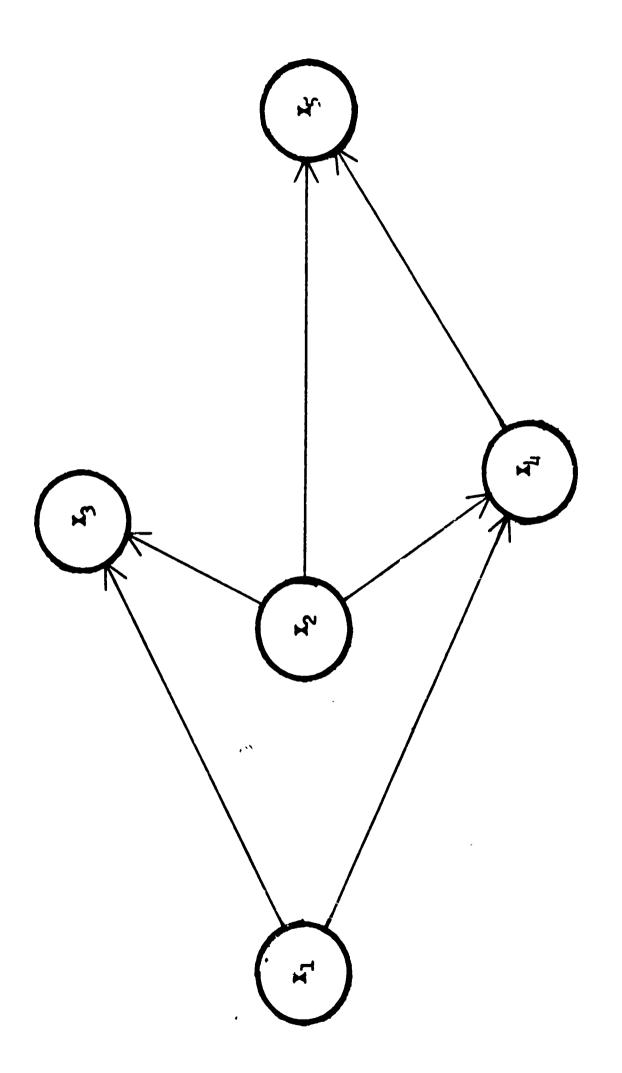
TRANSPARENCY 1-2

1

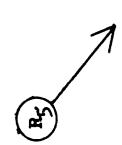
TRANSPARENCY 1-3

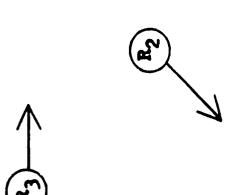


TRANSPARENCY 1-4



TRANSPARENCY 2-1









f Table 2

Beta Studies for Path 145

		Other I ₁				2,33
Comparisons	•	°		~ ~	mm	
	Direction 5-4-1	XS	-1,695	0355	-6250	0020
		x _L	6186 1,0279	8514 8274	1,080 907 1,080	6159 6024
		9'P	4093	0340	4014	0135
	Direction 1-4-5	ρŢ	275	262	262	गगा
		g/p	1127	6800	1104	0900
		\mathbf{x}_{l_1}	8720 9847	6755 6666	7989 9093	6728 6668
		X ₁	-1822	010	-2706	7600
		Other X	1	22	mm	2, 3 2, 3
Step			1	24	2B	3

TRANSPARENCY 3



GENERALIZATIONS ACAUSAL CAUSAL DIRECTION DIRECTION c-b-a a-b-c Comparing beta differentials, $|\beta_{ab \cdot k} - \beta_{ab \cdot kc}|$ Bobok - Boboka Then $< |\beta_{ac\cdot kb}|$ Bcarko and also, it follows that rbc*k rab·k And finally, r_{ab·kc} rbe • ka Known 3-variable causal direction in a closed system with k other system K variables operating. Also, from logical analysis, $|\mathbf{r}_{ac \cdot k'}| < |\mathbf{r}_{ab \cdot k''}|$ r_{bc•k}m < TRANSPARENCY 4

ERIC AFUITSAX Provided by ERIC